

RADICACIÓN

Problema 56:

Simplifica:

$$\left[\frac{2^n \cdot (2^{n-1})^n}{2^{n+1} \cdot 2^{n-1}} \cdot \frac{1}{4^{-n}} \right]^{1/n^2}$$

Solución Problema 56:

$$\begin{aligned} \left[\frac{2^n \cdot (2^{n-1})^n}{2^{n+1} \cdot 2^{n-1}} \cdot \frac{1}{4^{-n}} \right]^{1/n^2} &= \left[\frac{2^n \cdot 2^{n^2-n}}{2^n \cdot 2 \cdot 2^n \cdot 2^{-1}} \cdot \frac{1}{(2^2)^{-n}} \right]^{1/n^2} = \\ &= \left[\frac{\cancel{2^n} \cdot 2^{n^2} \cdot 2^{-n}}{\cancel{2^n} \cdot 2 \cdot 2^n \cdot \frac{1}{2}} \cdot \frac{1}{(2^2)^{-n}} \right]^{1/n^2} = \left[\frac{2^{n^2} \cdot 1}{2^n \cdot 2^n \cdot 2^{-2n}} \right]^{1/n^2} = \left[\frac{2^{n^2} \cdot \cancel{2^{2n}}}{\cancel{2^{2n}}} \right]^{1/n^2} = \\ &= [2^{n^2}]^{1/n^2} = \sqrt[n^2]{2^{n^2}} = 2 \end{aligned}$$

Luego,

$$\left[\frac{2^n \cdot (2^{n-1})^n}{2^{n+1} \cdot 2^{n-1}} \cdot \frac{1}{4^{-n}} \right]^{1/n^2} = 2$$