

PROBLEMAS DE TRIGONOMETRÍA

Problema 180:

Demostrar que si $a+b+c= 180^\circ$, se verifica:

$$\operatorname{tg} a + \operatorname{tg} b + \operatorname{tg} c = \operatorname{tg} a \cdot \operatorname{tg} b \cdot \operatorname{tg} c$$

Solución Problema 180:

$a+b+c= 180^\circ$ significa que son suplementarios, luego:

$$(a+b)= c$$

Por tanto,

$$\operatorname{tg}(a + b) = -\operatorname{tg} c$$

$$\frac{\operatorname{tg} a + \operatorname{tg} b}{1 - \operatorname{tg} a \cdot \operatorname{tg} b} = -\operatorname{tg} c$$

$$\operatorname{tg} a + \operatorname{tg} b = -\operatorname{tg} c(1 - \operatorname{tg} a \cdot \operatorname{tg} b)$$

$$\operatorname{tg} a + \operatorname{tg} b = -\operatorname{tg} c + \operatorname{tg} a \cdot \operatorname{tg} b \cdot \operatorname{tg} c$$

$$\operatorname{tg} a + \operatorname{tg} b + \operatorname{tg} c = \operatorname{tg} a \cdot \operatorname{tg} b \cdot \operatorname{tg} c$$