

## PROBLEMAS DE EXPRESIONES ALGEBRÁICAS Y OPERACIONES

### Problema 27:

Transforma y simplifica la expresión

$$\left(1 - \frac{2a}{2a + \frac{2}{a}}\right) a^3 + a$$

hasta que resulte= a

### Solución Problema 27:

$$\begin{aligned}\left(1 - \frac{2a}{2a + \frac{2}{a}}\right) a^3 + a &= \left(1 - \frac{2a^2}{2a^2 + 2}\right) (a^3 + a) \\ \left(1 - \frac{2a^2}{2(a^2 + 1)}\right) (a^3 + a) &= \left(1 - \frac{a^2}{a^2 + 1}\right) (a^3 + a) = \\ \left(1 - \frac{a^2}{a^2 + 1}\right) (a^3 + a) &= \left(\frac{a^2 + 1 - a^2}{a^2 + 1}\right) (a^3 + a) = \left(\frac{1}{a^2 + 1}\right) (a^3 + a) \\ \left(\frac{1}{a^2 + 1}\right) (a^3 + a) &= \left(\frac{1}{a^2 + 1}\right) a(a^2 + 1) = \frac{a(a^2 + 1)}{a^2 + 1} = a\end{aligned}$$